

Gravimetric calibration method for microflow

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Event: Workshop on microflow calibration methods (online)

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Microflow sizes

- Flow rates from 100 nL/min and down to 15 nL/min =>
6 mL/h to 0.9 μ L/h

Flow rate **100 nL/min**,
time to get the droplet: **50 min**

Flow rate **15 nL/min**,
time to get the droplet: **5.6 hours**



Water:

5 μ L \approx 5 mg

10 g Balance with 6 decimal places (μ g)

0.005000 g

5000 divisions (out of 1e7)

Gravimetric calibration method

Steady flow:

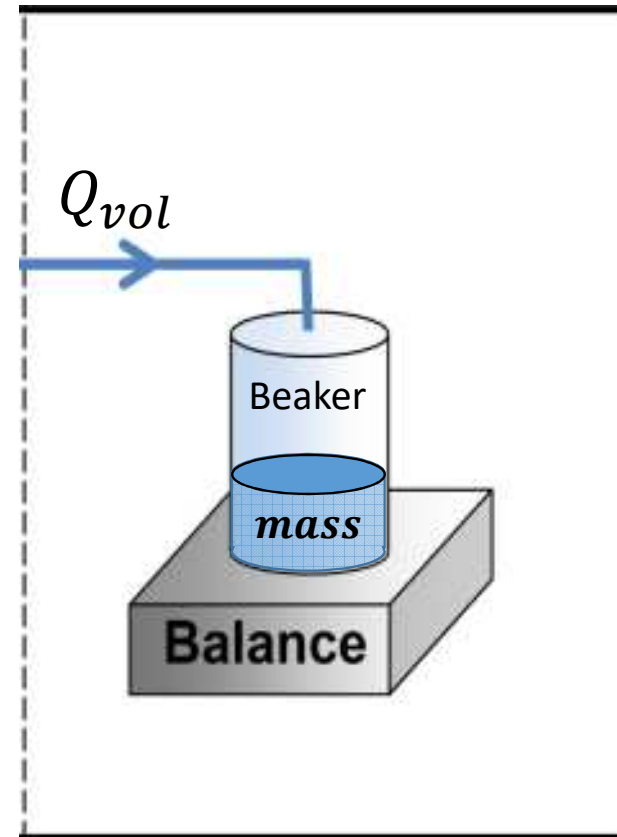
$$Q_{vol} = \frac{V_{delivered}}{\Delta time}$$

$$V_{delivered} = V_{finish} - V_{start}$$

$$\Delta time = t_{finish} - t_{start}$$

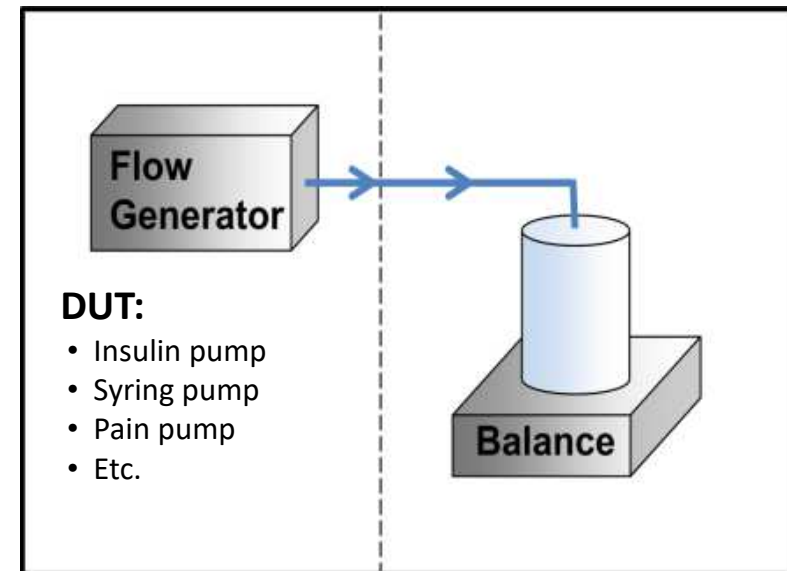
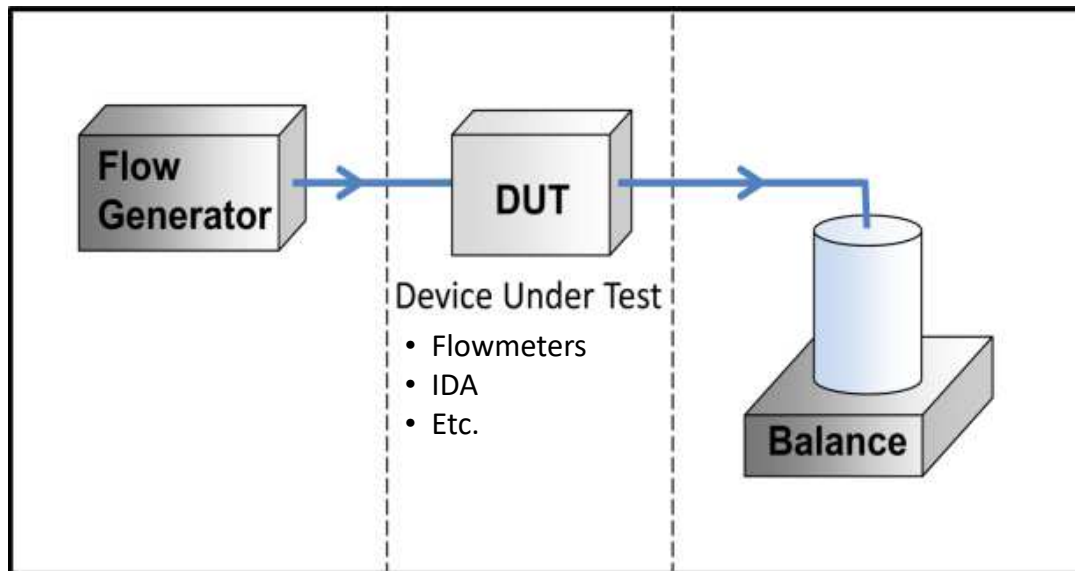
$$V = \frac{mass}{density}$$

Density is a function of temperature and is different from fluid to fluid



Gravimetric method

- The gravimetric method relies on weighing the mass of the working fluid delivered by or flowed through the DUT (Device Under Test) for a set time.
 - Steady flow (down to ≈ 15 nL/min)
 - Dynamic flow (down to ≈ 83 nL/min)



Parameters influencing the measurements

- Evaporation
- Water degassing
- Priming the tubing and the flow meter under test
- Flow rate stability
- Timing/measurement of time
- Temperature stability
- Buoyancy correction of the delivered liquid
- Buoyancy correction due to the immersed tube into the liquid
- Jet force out of the immersion tube
- Stick/slip of needle and liquid
- Drift and Linearity of the balance

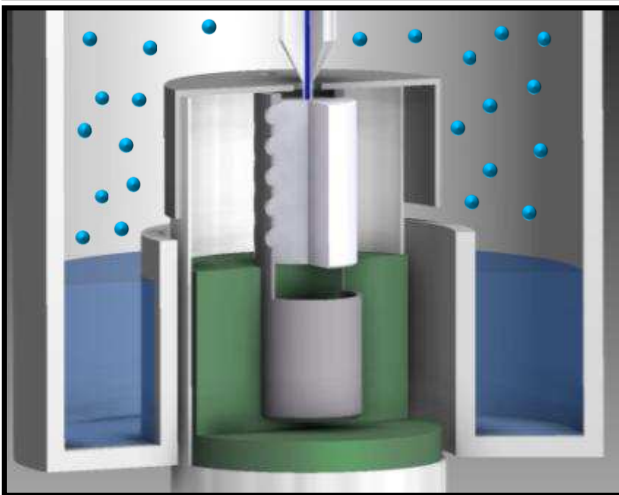
Evaporation traps

Evaporation rate from uncovered beaker is in the range of 40 nL/min which is more than the double of the lowest target flowrate of 15 nL/min.

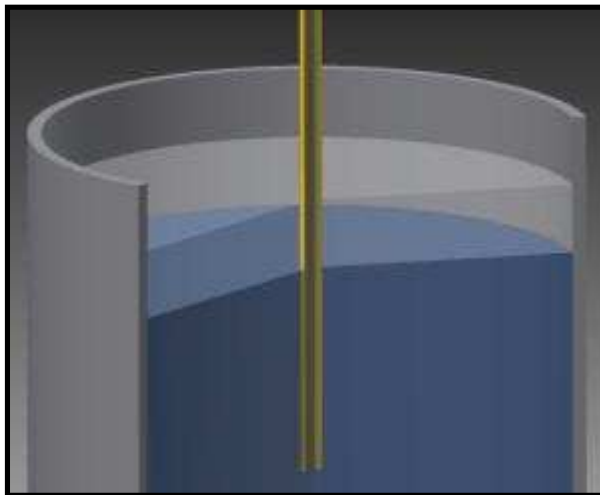
→ dependent on ambient condition as humidity, temperature etc.

→ With oil cover it can be lowered to 2-3 nL/min (must be adjusted for)

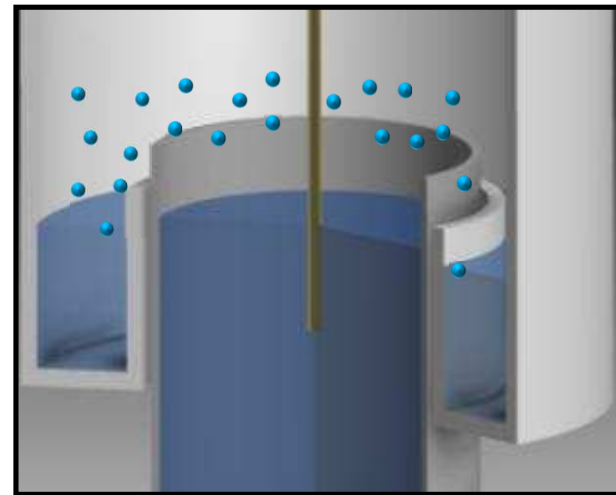
Water Bridge to water-absorbing materials in saturated air



Needle immersed into water with oil cover



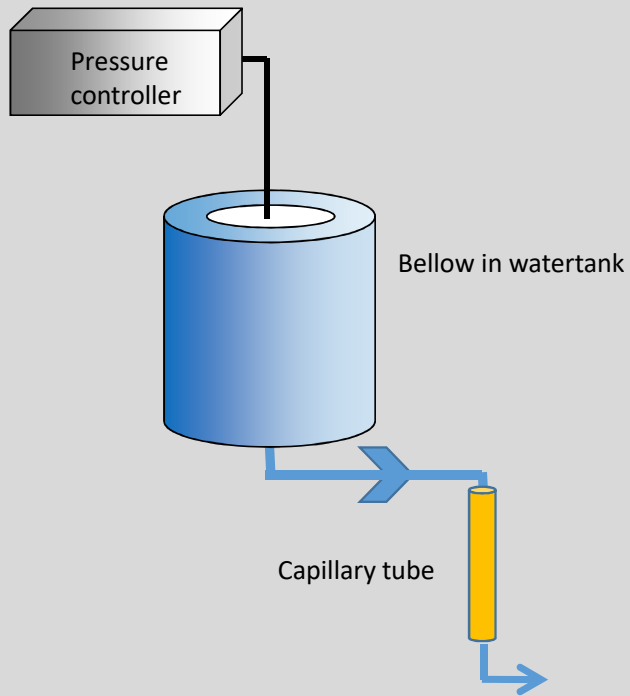
Needle immersed into water with saturated air around



Flow stability

- Generating flow

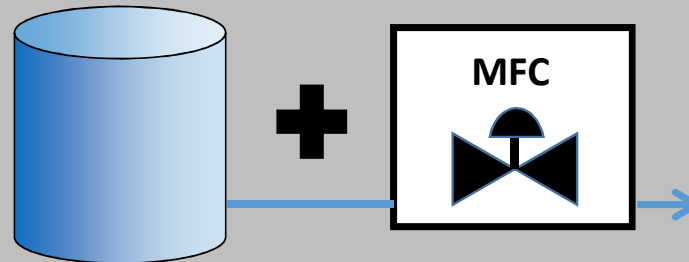
Constant pressure drop over capillary tube setting the flow rate



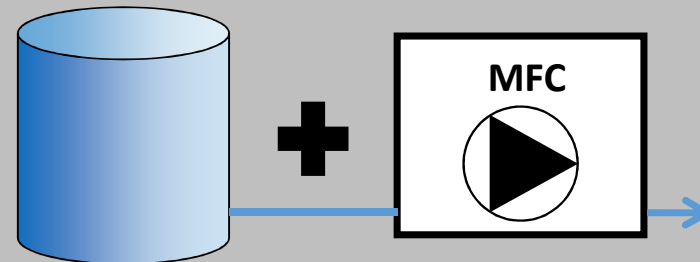
Syringe pump setting the flow rate



MFC setting the flow rate



MFC setting the flow rate

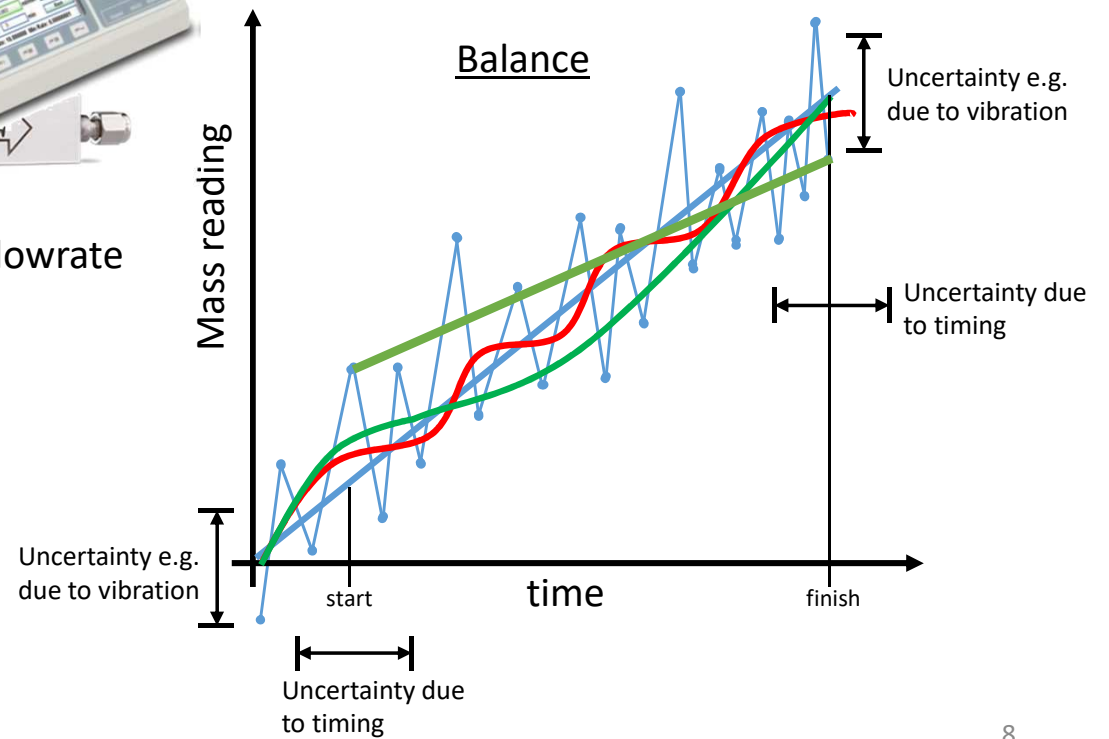
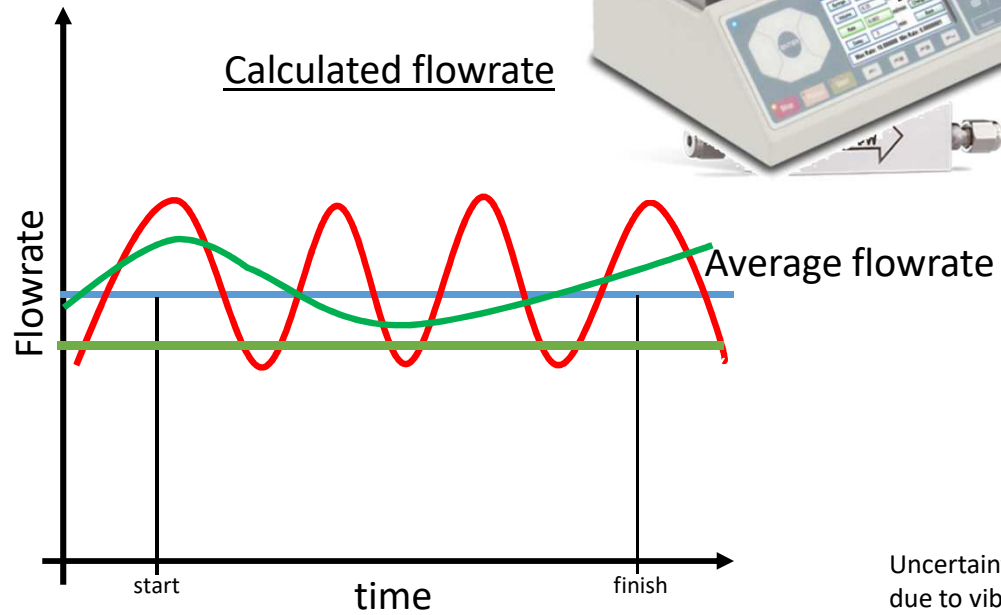


MFC = Mass Flow Controller

Flow and balance stability

$$\Delta mass = m_{finish} - m_{start}$$

$$Q_{average} = \frac{\Delta mass}{\Delta time}$$



Weighing

- *stability*

- Stable support – minimize vibration
 - (Granite table on flex support –rubber feet)
- Temperature stability
- Shielding against convection
- Avoid static electricity



Timing

- *Traceability*

- Steady flow

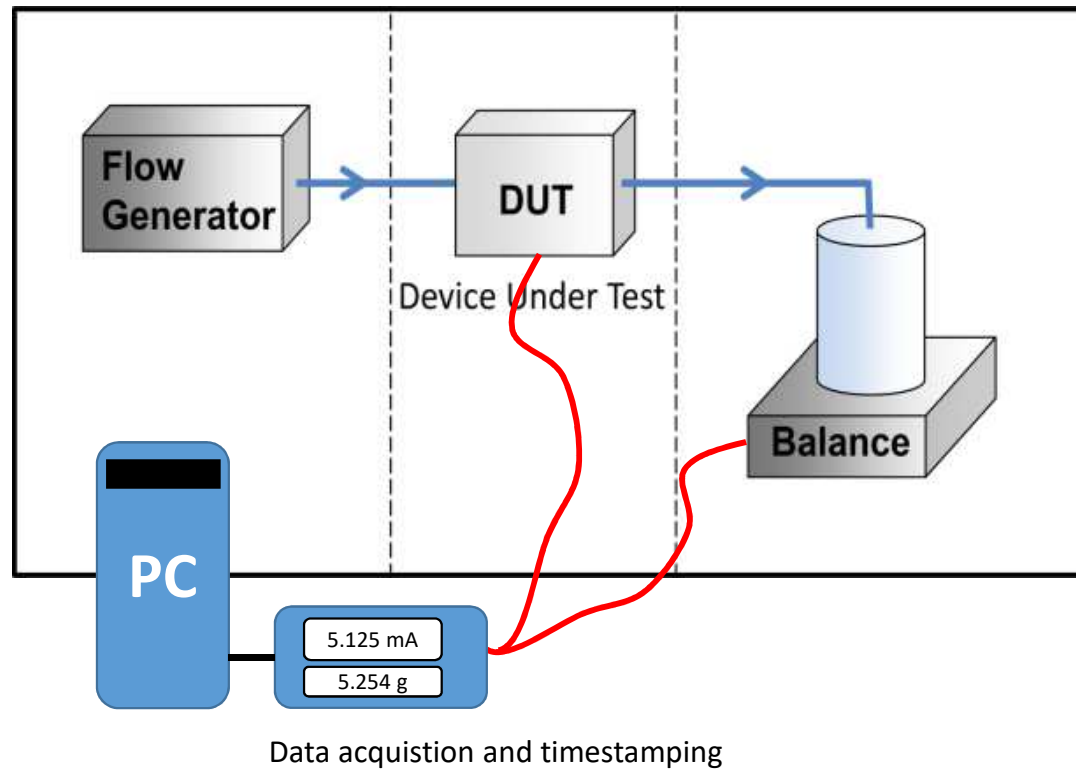
- $Q_v = \frac{\Delta V}{\Delta t} = \frac{\Delta(m/\rho)}{\Delta t}$

- Example:

- $\Delta t = 100 \text{ s}$
 - $u_t = 0.1 \text{ s}$
 - $\Rightarrow \frac{u_t}{\Delta t} = 0.1 \%$

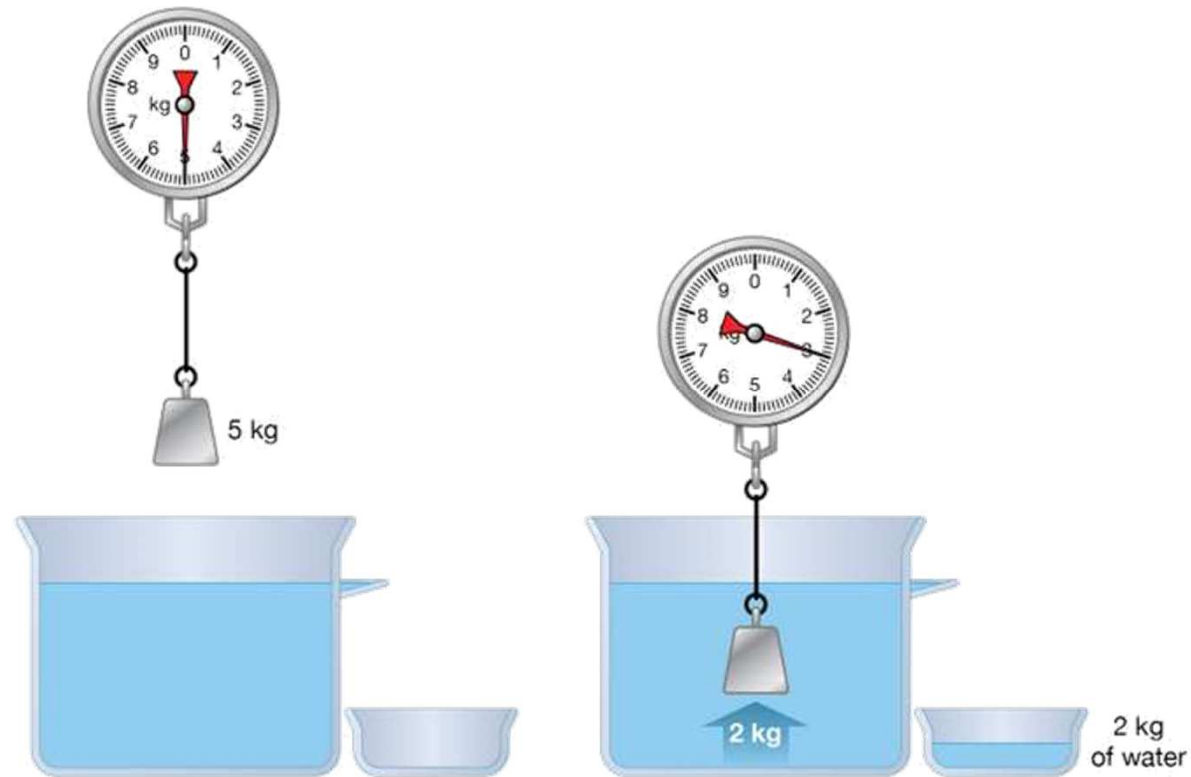
- Dynamic flow profile

- $dQ_v = \frac{d(m/\rho)}{dt}$



Buoyancy correction

Archimedes' principle



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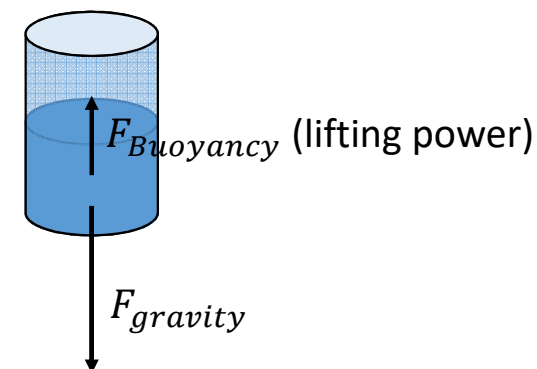
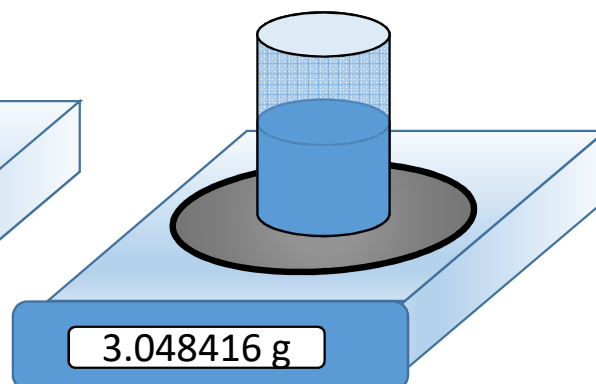
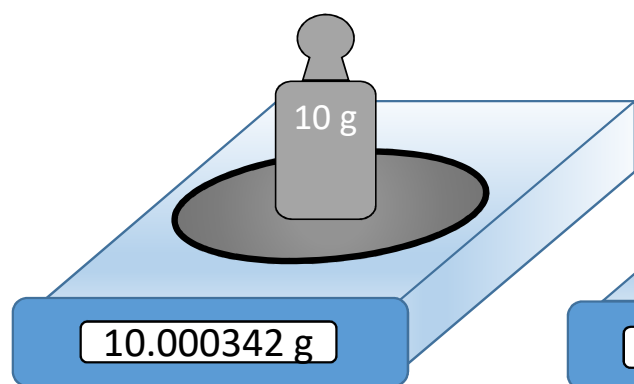
Buoyancy correction

- Buoyancy of the delivered liquid

$$m_{corr} = m_{uncorr} \cdot \frac{1 - \frac{\rho_{air}}{\rho_{weight}}}{1 - \frac{\rho_{air}}{\rho_{liquid}}}$$

ρ_{air} is a function of air temperature, barometric pressure and humidity

ρ_{liquid} is a function of temperature

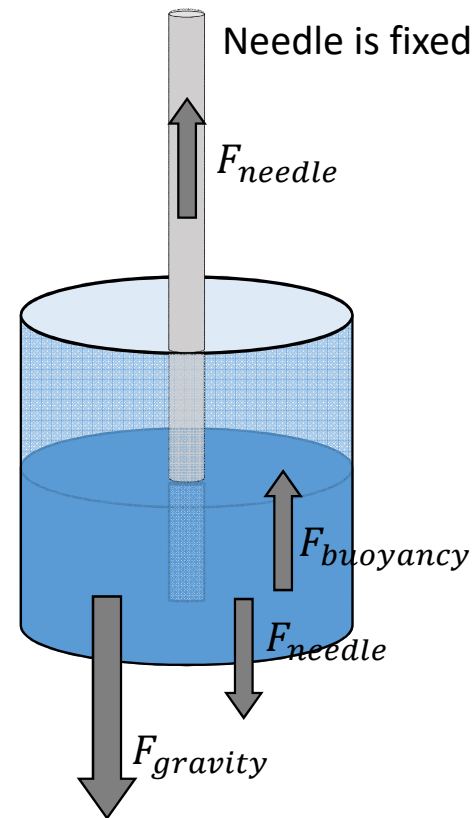


Buoyancy correction

- Immersion of tube into the liquid

It's only necessary to calculate buoyancy corrections for Δmass

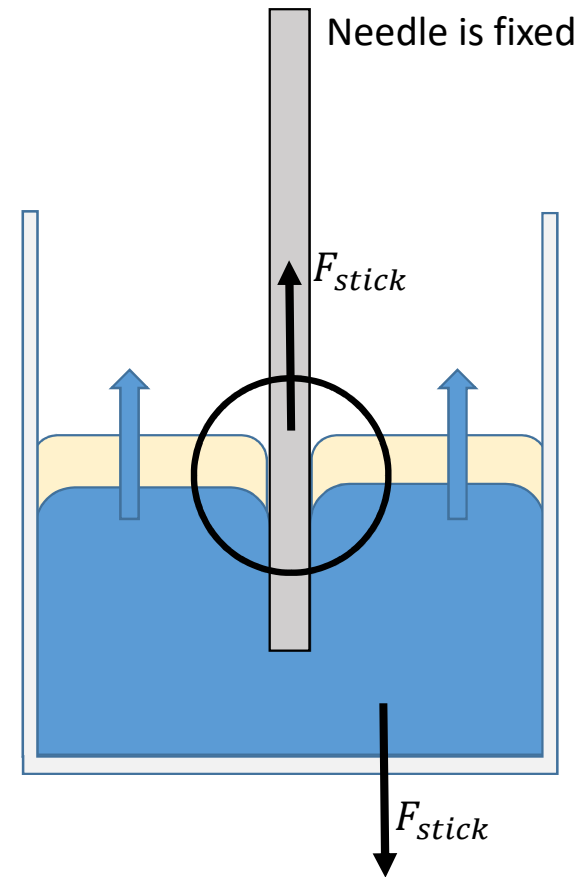
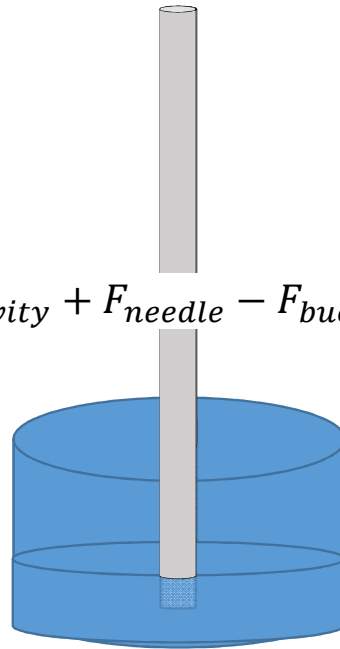
$$F_{total} = F_{gravity} + F_{needle} - F_{buoyancy}$$



Buoyancy correction

- Immersion of tube into the liquid

$$F_{total} = F_{gravity} + F_{needle} - F_{buoyancy} + F_{stick}$$



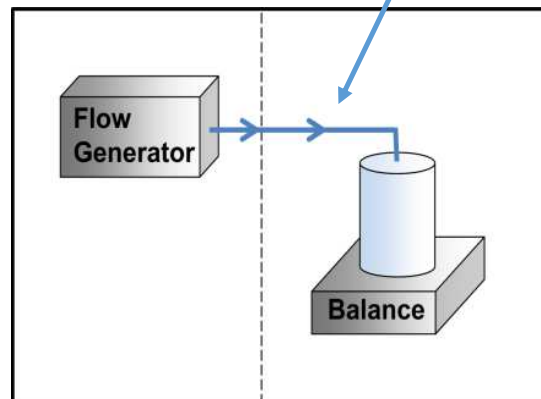
Temperature stability I

Effects of changing temperature:

- Weighing/balance
- Flow-meter reading
- Mass flow vs. Volume flow
- Flow generated by expansion

Flow generated by expansion

- Example: 1 m SS tube, ID = 1 mm
- Temperature: 23 °C → 24 °C
 - Water: $\Delta V = 121$ nl
 - Tube: $\Delta V = -12$ nl
 - Sum: $\Delta V = 109$ nl
 - If $\Delta t = 6$ min → flow ≈ 17 nL/min

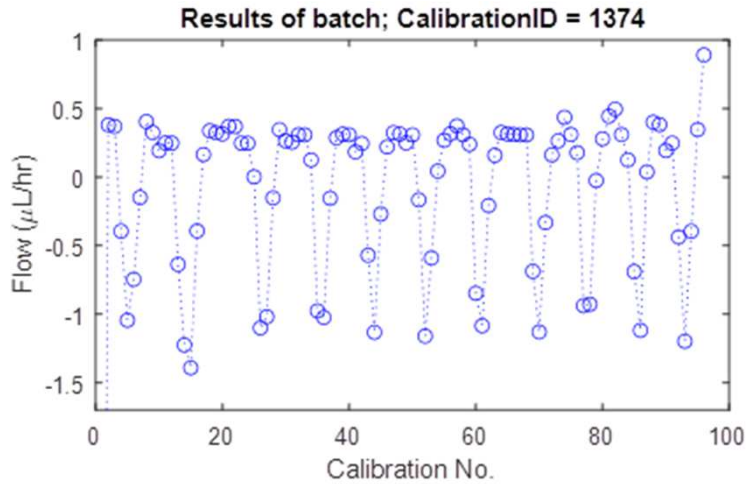


Temperature stability II

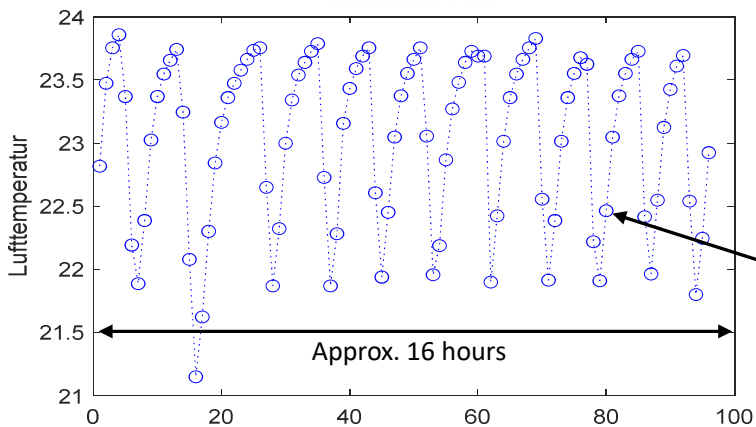
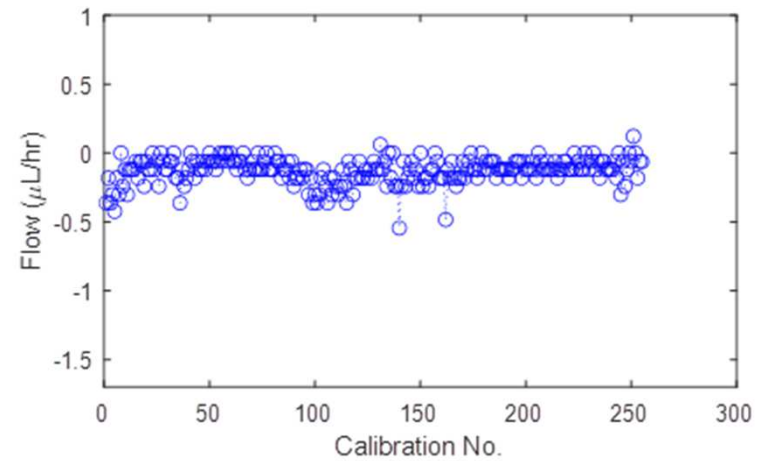
(before insulation)



(after insulation)



**Pump
stopped!**



Air conditioning

Resolution (for 10 min measurement):

$$\frac{1 \mu\text{g}}{10 \text{ min}} \sim 0.001 \frac{3600}{600} = 0.06 \mu\text{L/hr}$$

Temperature stability III



Temperature stability IV:

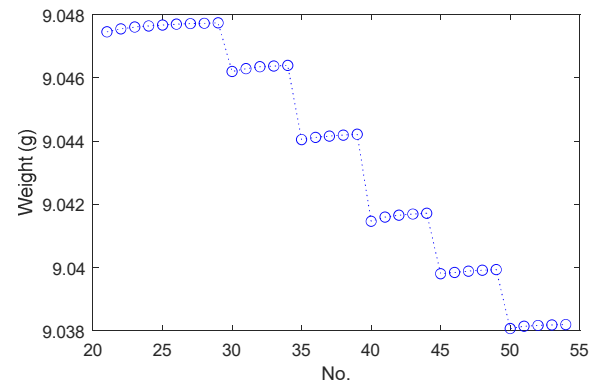
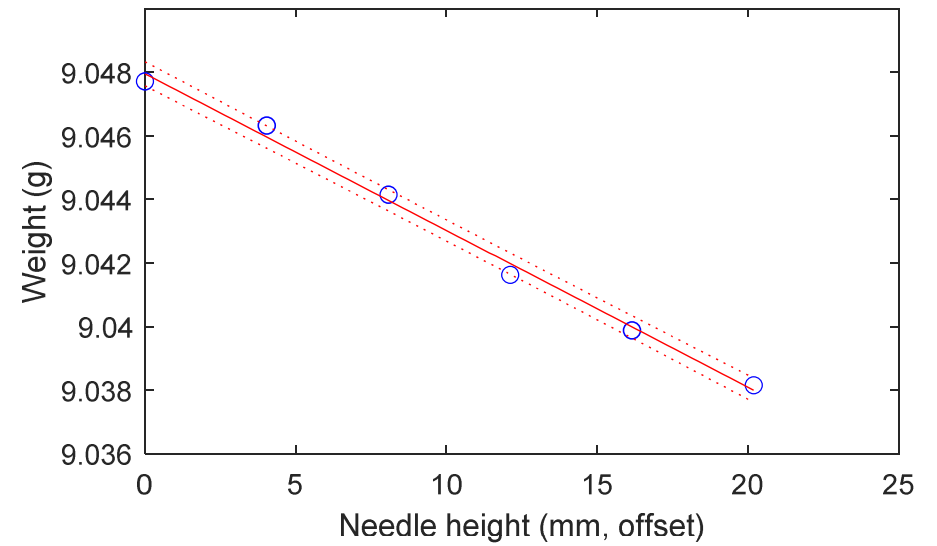
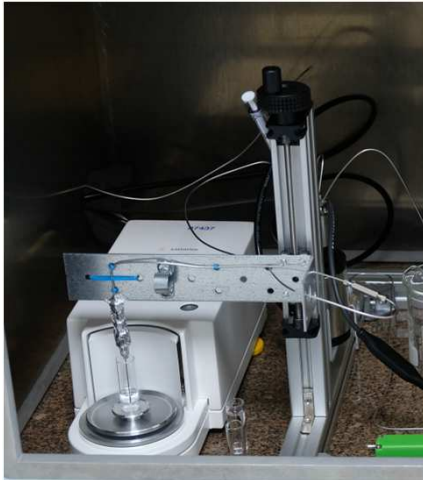
- *What can we do?*

- ✓ Stabilize lab temperature
 - ✓ Large heat capacity
 - ✓ Heat conducting shield (→ isotherm)
 - ✓ Isolating screen
-
- Short tubes with small ID (Inner Diameter)
 - Stabilization of setup by water cooling/heating



Displacement by needle

Check: Weight vs needle height

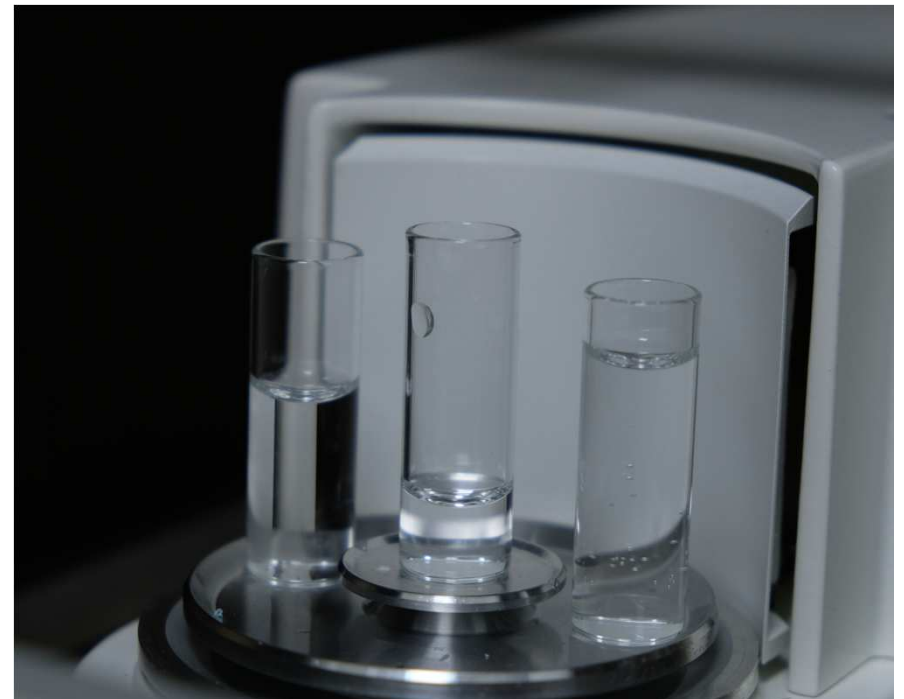


Emptying the beaker I:

- What do we do when the beaker is full?

- Option 1: Replace with a new
 - Manual process
 - Thermal perturbation
 - in practice: only small flows
- Option 2: Pump out
 - Automatic process
 - Thermal steady state
 - Increased flow rate

DTI $\rightarrow \Delta m \approx 4 \text{ g} \Rightarrow Flow_{max} \approx 1 \text{ ml/min}$

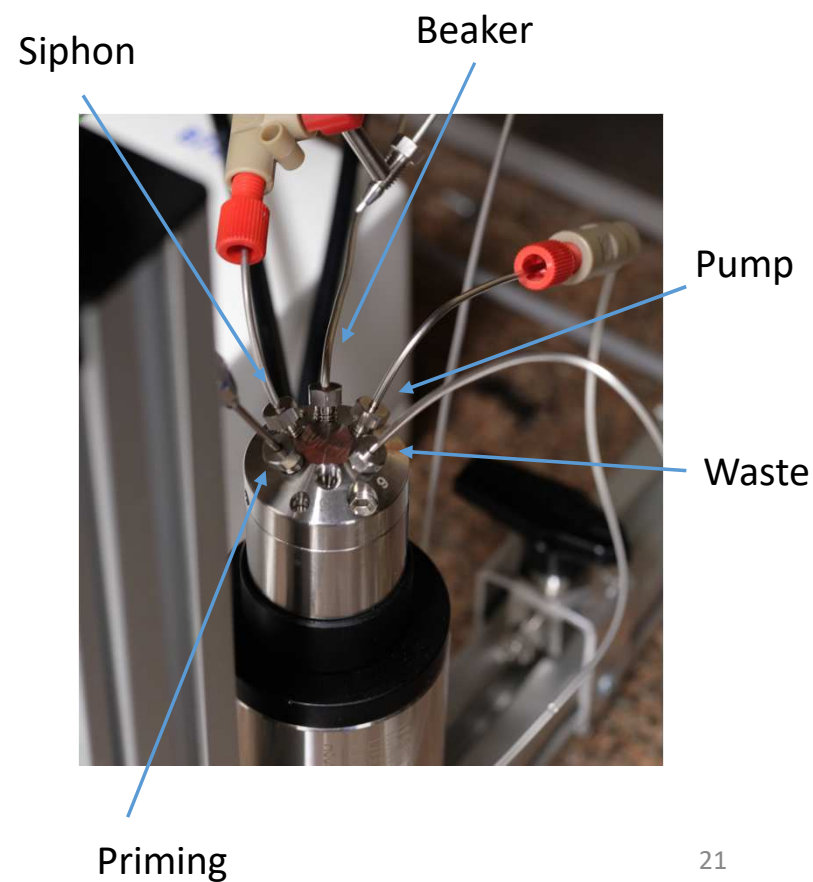
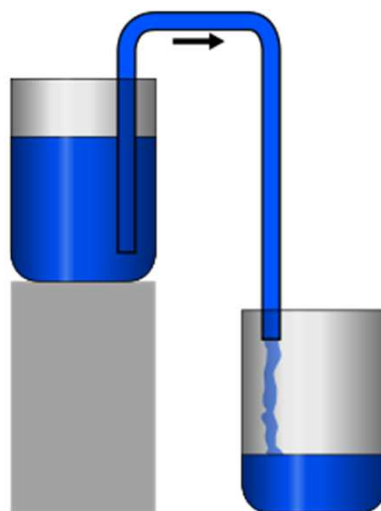


Emptying the beaker II:

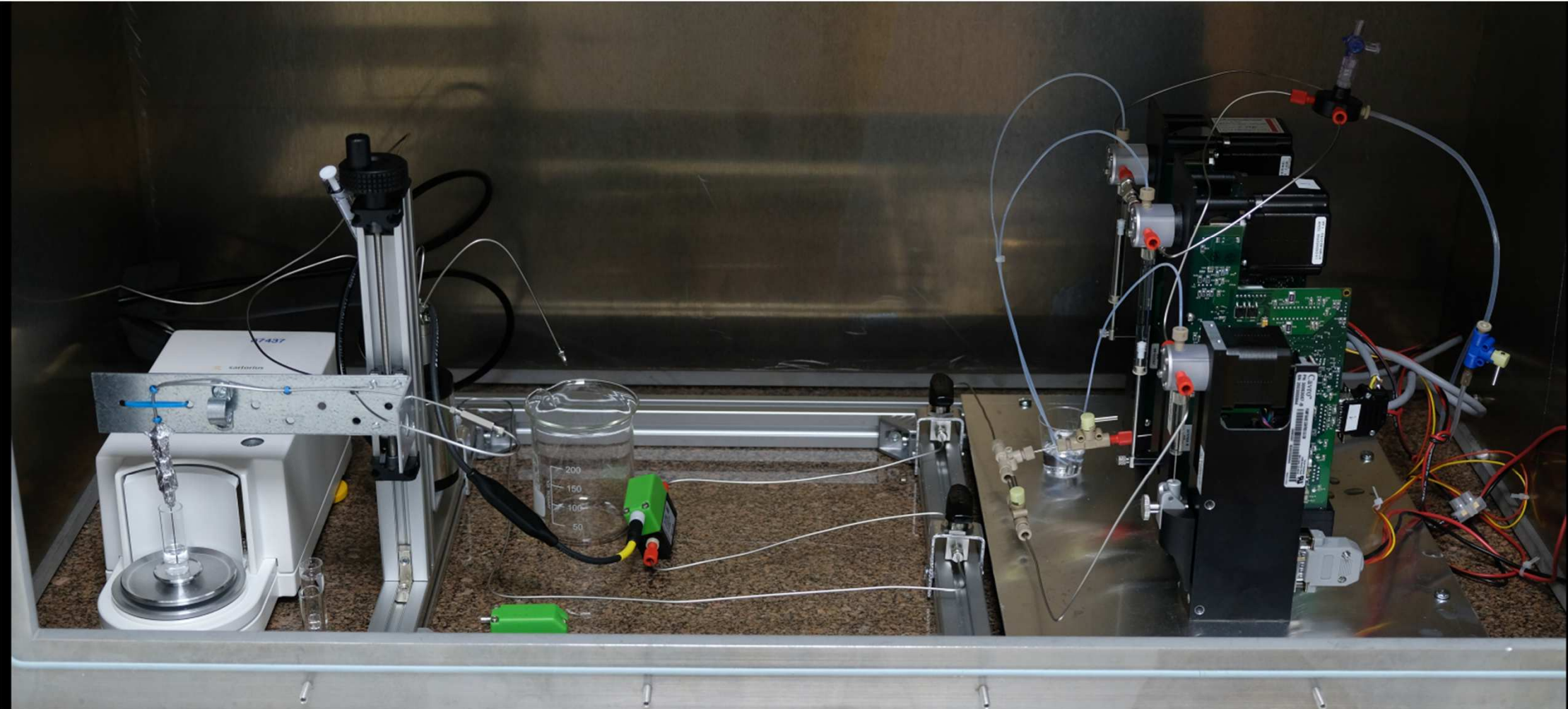
- Example of beaker pumping system

- Siphon
- Control: 6-port valve
- Control signal: Weight
 - 9.5 g → Empty
 - 5.5 g → Fill

Alternative: Insert separate needle / syringe (-pump)



Example of setup (DTI)



Project Team



UMC Utrecht

INESC MN

Microsystems and
Nanotechnologies



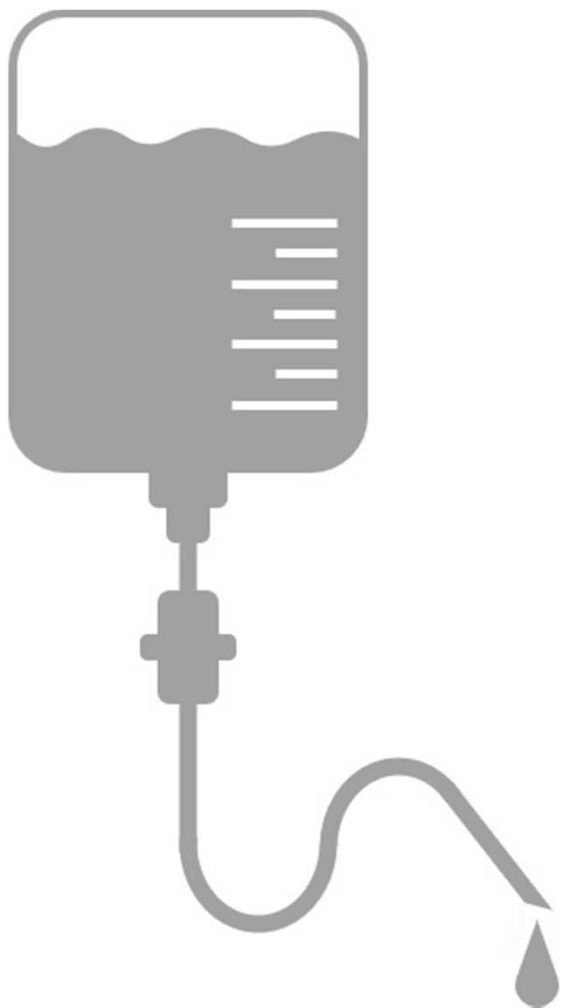
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THANK YOU

